

## Circuit Diagrams and Kirchhoff's Laws

Homework:

p478 Q31

$$I = 7.60 \text{ A}$$

$$240 \text{ V}$$

$$\text{rate of water} = ? = m/t$$

$$\text{change in temperature} = 6^\circ \text{C}$$

$$Q = mc\Delta T$$

$$P = VI = Q/t$$

$$VI = (m/t)c\Delta T$$

$$m/t = VI/c\Delta T$$

$$m/t = 240 \times 7.6 / (4180 \times 6) = 0.0727 \text{ kg/s}$$

Q9

$$I = 1.0 \text{ A} = \frac{Q}{t} = \frac{\rho V}{t}$$

$$r = 1.0 \text{ mm}$$

$$\rho = \frac{Q}{V} = 10^{29} \frac{e^-}{\text{m}^3}$$

$$V = \pi r^2 \Delta L$$

$$I = \frac{\rho V}{t} = \pi r^2 \rho \frac{\Delta L}{t}$$

$$I = \pi r^2 \rho v$$

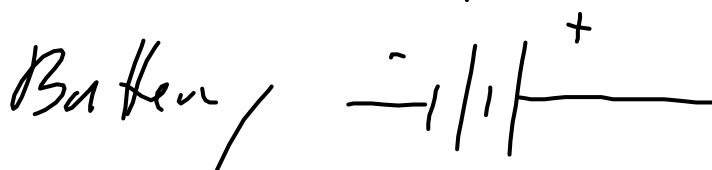
$$v = \frac{I}{\pi r^2 \rho} = \frac{1.0 \text{ A} \left( \frac{e^-}{1.6 \times 10^{-19} \text{ C}} \right)}{\pi (1.0 \text{ mm})^2 (10^3 \frac{\text{m}}{\text{m}^3})}$$

$$v = 2.0 \times 10^{-5} \text{ m/s}$$

Circuit diagrams:

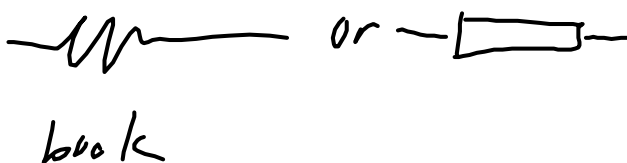
electrochemical cell:

negative ← long line = positive



Wire

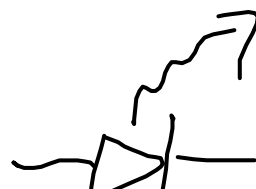
resistors



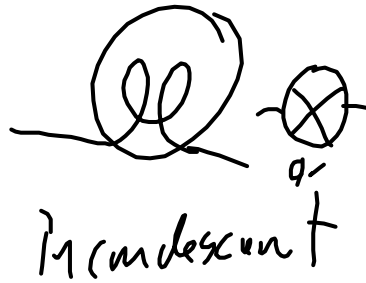
Variable resistor  
or rheostat or potentiometer



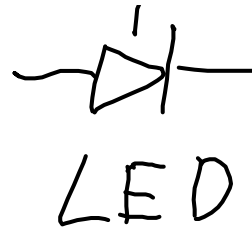
1. 1. 1.



lights



incandescent



ammeter - measures current

ALWAYS PUT AMMETERS IN SERIES

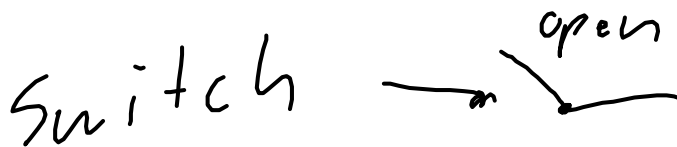


Voltmeter - measures potential difference between two points in the circuit.

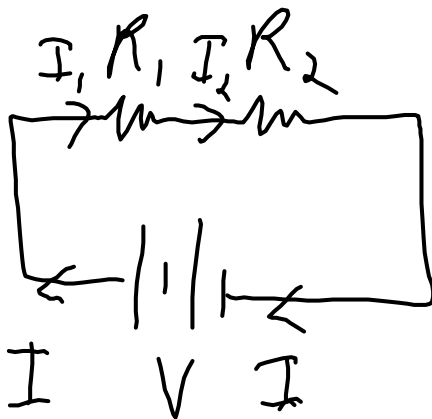
Put the voltmeter in parallel across the element you are measuring.



Galvanometer - measures very small currents.



Let's look at series and parallel circuits



$$\frac{V}{I} = R_T$$

↑  
equivalent  
resistance

$$R_T = R_1 + R_2 \text{ in series}$$

What is the current through  $R_1$  and  $R_2$ ?

Same as  $I = I_1 = I_2$  series

How about voltage?

$$V_1 = IR_1 \quad V_2 = IR_2$$

by conservation of energy

$$P_{\text{Battery}} = VI = P_{R_1} + P_{R_2}$$

$$VI = V_1 I + V_2 I$$

Kirchhoff's  $\rightarrow$   $V = V_1 + V_2$

Loop law

- voltages around a loop add to zero

Parallel Circuits



By law of conservation of charge

$$Q_{\text{in}} = Q_{\text{out}}$$

$$I_{\text{in}} = I_{\text{out}}$$

$$+ V \quad \boxed{I_{in} = I_{out}}$$

Kirchoff's Junction Law

$$\boxed{I = I_1 + I_2} \quad \text{Parallel}$$

$$P = P_1 + P_2$$

$$VI = V_1 I_1 + I_2 V_2$$

therefore  $\boxed{V = V_1 = V_2}$  Parallel

$$I = I_1 + I_2$$

$$\frac{V}{R_T} = \frac{V_1}{R_1} + \frac{V_2}{R_2}$$

$$\boxed{\frac{1}{R_T} = \frac{1}{R_1} + \frac{1}{R_2}} \quad \text{Parallel}$$

e.g. You connect a 6.00V  
Battery to a  $350\Omega$

resistor and a 100  $\Omega$  resistor,  $\uparrow$  354)

Determine the voltage across, current through and power output of each resistor when they are  
a) in series with each other  
b) in parallel with each other

Draw a circuit diagram showing an ammeter and voltmeter connected to the 100 ohm resistor.

p499-500 Q1-11 odds

q 5 and 11 - redraw the diagram to show series and parallel parts

Lab next Thursday p85-89 Kirchhoff's laws and series and parallel circuits

Q31

$$I = 7.6A, V = 240V$$

$$\Delta T = 6^{\circ}C \quad c = 4180 \text{ J/kg}^{\circ}C$$

$$\text{rate} = m/t$$


$$P = VI = Q/t$$

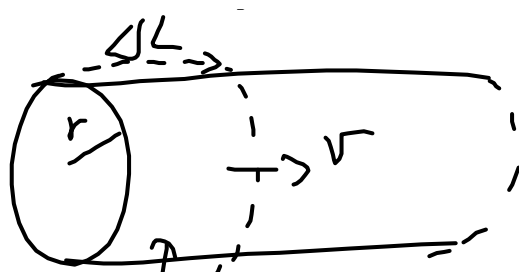
$$Q = mc\Delta T$$

$$VI = (mc\Delta T)/t$$

$$VI/c\Delta T = m/t = 240 \times 7.6 / (4180 \times 6) = 0.0727 \text{ kg/s}$$

Q9

$$I = 1.0A = \frac{Q}{t}$$




$$\rho = \frac{10^{29} e^-}{m^3} = \frac{Q}{V} \rightarrow Q = \rho V$$

$$V_{\text{cylinder}} = \pi r^2 \Delta L$$

$$I = \frac{Q}{t} = \frac{\rho V}{t} = \pi r^2 \rho \left( \frac{\Delta L}{t} \right)$$

$$I = \pi r^2 \rho v$$

$$v = \frac{I}{\pi r^2 \rho} = \frac{1.0 A}{\pi (1 \text{ km})^2 \frac{10^{29}}{m^3} (1.6 \times 10^{-19} \frac{C}{e^-})}$$

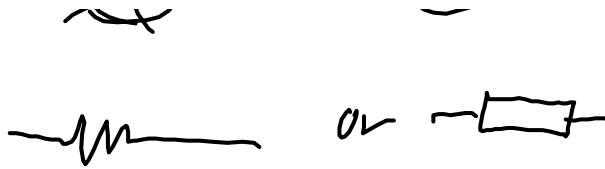
$$\boxed{2.0 \times 10^{-5} \text{ m/s}}$$

Circuits  
Symbols:

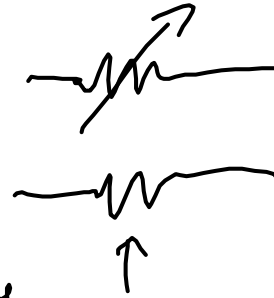
light bulb



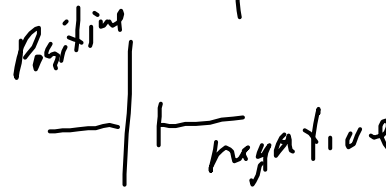
resistor:



variable resistor  
(rheostat or potentiometer)

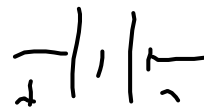


Electrochemical cell



current usually flows out of the positive end  
and into the negative end, equally  
(conservation of charge, charge out=charge  
in or current out=current in).

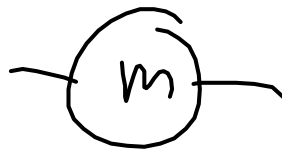
battery



wire



motor



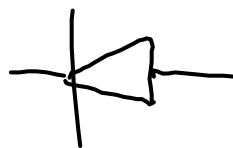
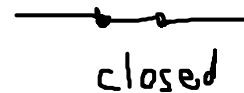
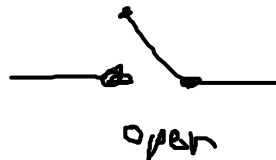
Or



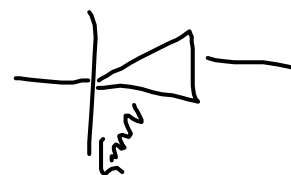
armature  
*armature*

*13 magnetic field*

switch



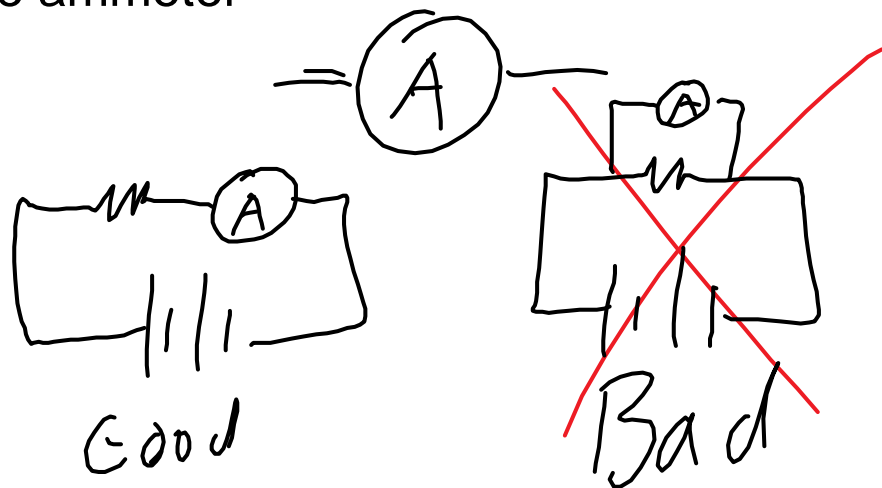
Diode



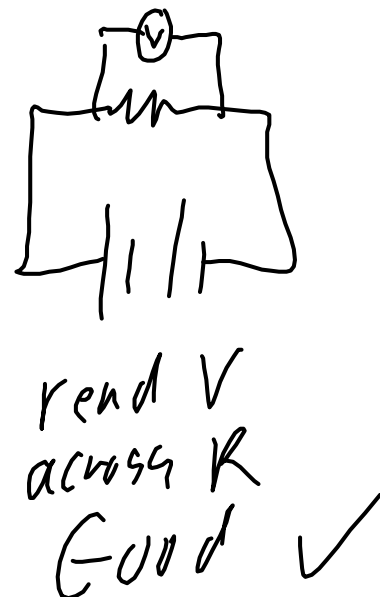
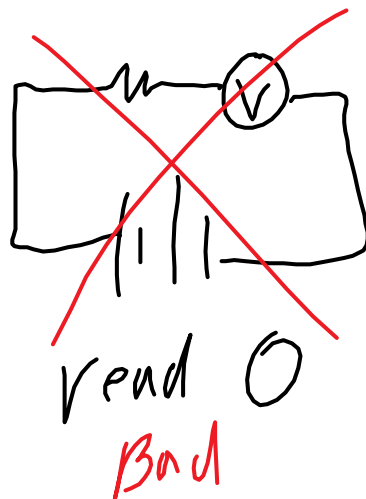
LED



Ammeters - measures current  
**MUST BE CONNECTED IN SERIES**- or you  
 can fry the ammeter



Voltmeter - measure potential difference  
 between two points on the circuit.  
 In parallel with the element measured.



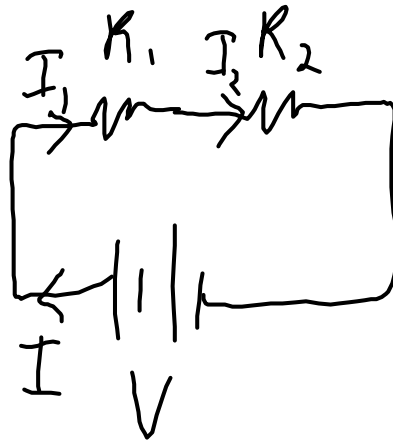
Galvanometer - measures small currents



Look at series and parallel circuits and voltage,  
 current, resistance and power.

Series  $, R_1, I, R_2$

Series



$I = I_1 = I_2$   
no charge  
is lost

By conservation of energy

$$P_{in} = P_{out}$$

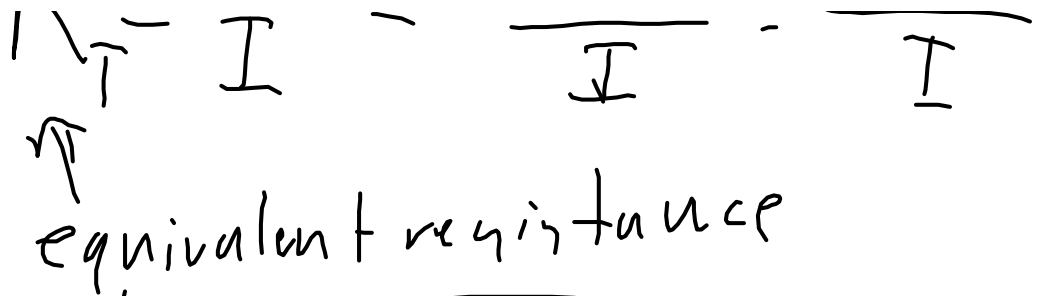
$$VI = \underbrace{V_1 I}_{\substack{\text{energy} \\ \text{given off} \\ \text{by resistor 1}}} + \underbrace{V_2 I}_{\substack{\text{resistor} \\ 2}}$$

$$\boxed{V = V_1 + V_2} \text{ Series}$$

Kirchhoff's loop law -

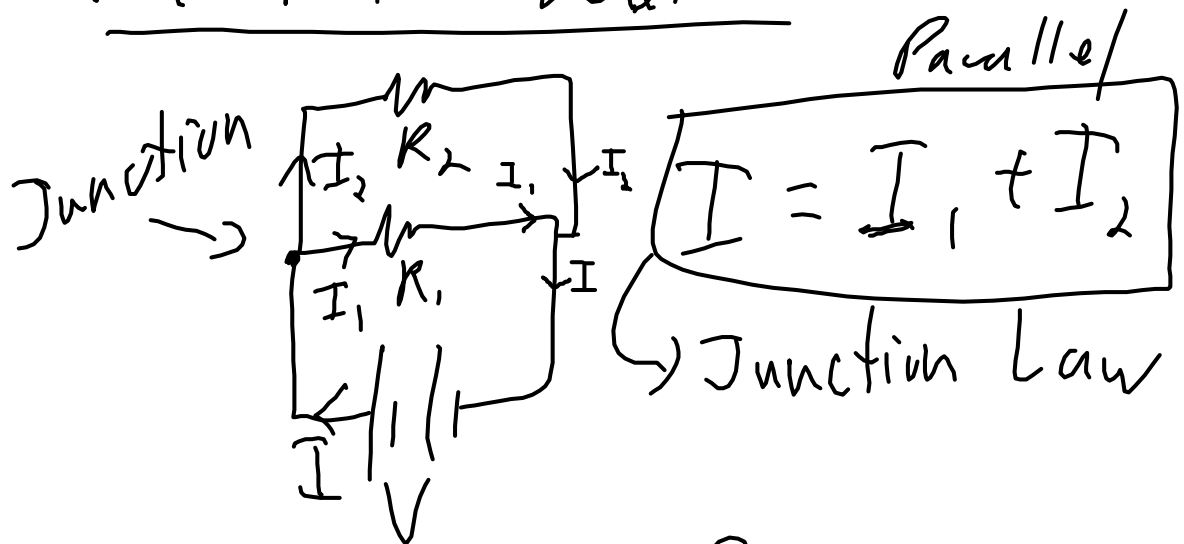
Voltages around a loop  
add to zero ( $V_{in} = V_{out}$ )

$$R = \frac{V}{I} = \frac{V_1 + V_2}{I} = \frac{R_1 I + R_2 I}{I}$$



$$\boxed{R_T = R_1 + R_2} \text{ Series}$$

## Parallel circuits



$$P_{in} = P_{out}$$

$$VI = I_1 V_1 + I_2 V_2$$

$$I = I_1 + I_2$$

$$\boxed{V = V_1 = V_2} \text{ Parallel}$$

Circuit elements in parallel

diff. have the same potential

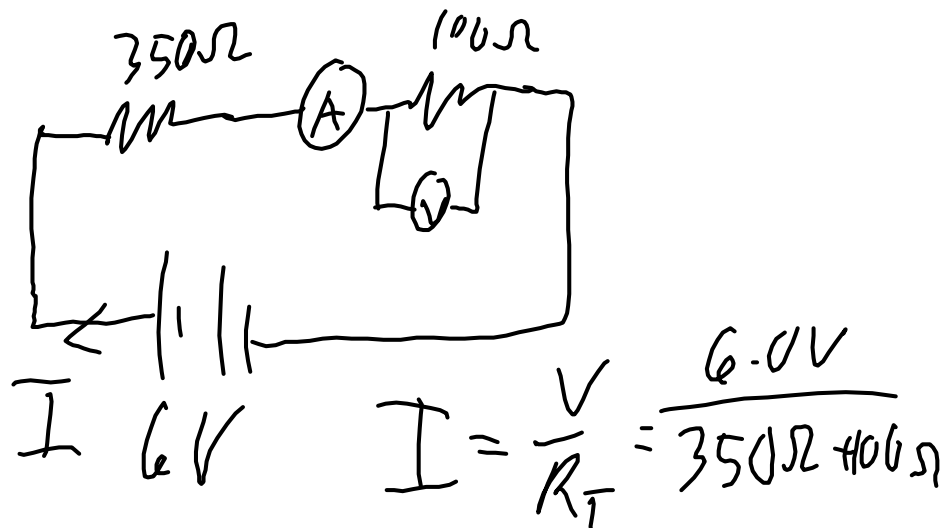
$$I = I_1 + I_2$$

$$\frac{V}{R_T} = \frac{V_1}{R_1} + \frac{V_2}{R_2}$$

$$\boxed{\frac{1}{R_T} = \frac{1}{R_1} + \frac{1}{R_2}} \text{ Parallel}$$

- Determine the voltage across, current through and power output of each resistor when they are
- in series with each other
  - in parallel with each other

Draw a circuit diagram showing an ammeter and voltmeter connected to the 100 ohm resistor.



$$= 13.3 \text{ mA}$$

$$V_{350} = I R = 350 \Omega \times 13.3 \text{ mA}$$

$$= \boxed{4.67 \text{ V}}$$

$$V_{100\Omega} = 100 \Omega \times 13.3 \text{ mA}$$

$$= \boxed{1.33 \text{ V}}$$

$$P_{350\Omega} = I^2 R = (13.3 \times 10^{-3})^2 (350)$$

$$= \boxed{62.2 \text{ mW}}$$

$$P_{100\Omega} = \boxed{17.8 \text{ mW}}$$